

Question Number	Answer	Mark
1(a)	Correct conversion of lb to kg (1) Use of $W = mg$ with $g/6$ (1) $W_{\text{moon}} = 26 \text{ N}$ (1) <u>Example of calculation</u> $35 \text{ lb} = 35 \text{ lb} \times 0.45 = 15.75 \text{ kg}$ $g_{\text{moon}} = 9.81 \text{ N kg}^{-1}/6 = 1.635 \text{ N kg}^{-1}$ $W_{\text{moon}} = 15.75 \text{ kg} \times 1.635 \text{ N kg}^{-1}$ $W_{\text{moon}} = 25.8 \text{ N}$	3
1(b)	Divide by six (1)	1
1(c)	Spring used on Earth has to be stiffer Or have a greater spring/stiffness constant (1) (Accept converse for the spring on the moon) To give the same extension for (the same mass) (1)	2
Total for Question		6

Question Number	Answer	Mark
2(a)	Use of $g = \frac{GM}{r^2}$ (1) $M = 4.5 \times 10^{23} \text{ kg}$ (1) <u>Example of calculation</u> $M = \frac{gr^2}{G} = \frac{9.81 \text{ N kg}^{-1} \times (1.74 \times 10^6 \text{ m})^2}{6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}} = 4.45 \times 10^{23} \text{ kg}$	2
2(b)	(the gravitational force on the Moon would be larger), but the centripetal acceleration would be independent of the mass of the Moon Or $r\omega^2 = \frac{GM}{r^2} \quad \therefore \omega^2 = \frac{GM}{r^3}$ (1) (angular) velocity and hence T is independent of mass of Moon (1)	2
2(c)	Gravitational forces on the seas/oceans/Earth would be greater (1) Or Tidal variations would be more extreme [accept tides would be bigger, higher, larger, faster; do not accept tides would be stronger]	1
Total for Question		5

Question Number	Answer	Mark
3(a)(i)	<p>Use of $\omega = \frac{2\pi}{T}$ (1)</p> <p>See $F = \frac{GMm}{r^2}$ and $F = m\omega^2 r$ (1)</p> <p>$GM = 4.07 \times 10^{14} \text{ (m}^3 \text{ s}^{-2}\text{)}$ (1)</p> <p>Or</p> <p>Use of $v = \frac{2\pi r}{T}$ (1)</p> <p>See $F = \frac{GMm}{r^2}$ and $F = \frac{mv^2}{r}$ (1)</p> <p>$GM = 4.07 \times 10^{14} \text{ (m}^3 \text{ s}^{-2}\text{)}$ (1)</p> <p>[If reverse “show that” attempted, max 2]</p> <p><u>Example of calculation:</u></p> $\omega = \frac{2\pi}{T} = \frac{2\pi \text{ rad}}{2.36 \times 10^6 \text{ s}} = 2.66 \times 10^{-6} \text{ rad s}^{-1}$ $\frac{GMm}{r^2} = m\omega^2 r$ $GM = \omega^2 r^3 = (2.66 \times 10^{-6} \text{ s}^{-1})^2 \times (3.86 \times 10^8 \text{ m})^3 = 4.07 \times 10^{14} \text{ m}^3 \text{ s}^{-2}$	3
3(a)(ii)	<p>Use of $g = \frac{GM}{R^2}$ with $g = 9.81 \text{ N kg}^{-1}$ (1)</p> <p>$R = 6.4 \times 10^6 \text{ m}$ [$6.5 \times 10^6 \text{ m}$ if show that value used] (1)</p> <p><u>Example of calculation:</u></p> $R = \sqrt{\frac{GM}{g}} = \sqrt{\frac{4.07 \times 10^{14} \text{ m}^3 \text{ s}^{-2}}{9.81 \text{ N kg}^{-1}}} = 6.44 \times 10^6 \text{ m}$	2

3(b)	Force varies with distance (from the Earth) according to inverse square law		
	$F \propto \frac{1}{r^2}$	(1)	
	so force (on these asteroids) is (very) small	(1)	
	Or		
	Gravitational field strength varies with distance (from the Earth) according to inverse square law $g \propto \frac{1}{r^2}$	(1)	
	so gravitational field strength is (very) weak at this distance	(1)	2
	[Accept idea that since the asteroids are much further from the Earth (than the moon) they are only weakly bound (to the Earth) for max 1 mark]		
Total for Question			7

Question Number	Answer	Mark
4	Use of $F = \frac{Gm_1m_2}{r^2}$	(1)
	$F = 8.2 \times 10^{16} \text{ N}$	(1)
	<u>Example of calculation:</u>	
	$F = \frac{Gm_1m_2}{r^2} = \frac{6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2} \times 6.4 \times 10^{23} \text{ kg} \times 6.0 \times 10^{24} \text{ kg}}{(5.6 \times 10^{10} \text{ m})^2}$ $F = 8.17 \times 10^{16} \text{ N}$	
		2

Question Number	Answer	Mark
5(a)	See $F = mg$ and $F = (-)GmM/r^2$ Equate and cancel m on either side	(1) (1) 2
5(b)	Substitute into $g = GM/r^2$ to obtain $g = 9.78 \text{ N kg}^{-1}$ [condone m s^{-2}] <u>Example of calculation</u> $g = \frac{GM}{r^2} = \frac{6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2} \times 5.97 \times 10^{24} \text{ kg}}{(6.38 \times 10^6 \text{ m})^2} = 9.783 \text{ N kg}^{-1}$	(1) 1
Total for question		3

Question Number	Answer		Mark
6(a)	The gravitational field strength [accept “g”] decreases Or the (gravitational) force on the satellite/object/mass decreases It is a centripetal force (and not a centrifugal force) The satellite is accelerating and so is not in balance	(1) (1) (1)	3
6(b)(i)	See $\frac{mv^2}{r} = \frac{GmM_E}{r^2}$ Or $m\omega^2 r = \frac{GMm}{r^2}$ $\therefore v^2 = \frac{GM_E}{r}$ Or $v = \sqrt{\frac{GM_E}{r}}$ GM _E is constant (and so v decreases as r increases) Or $v^2 \propto \frac{1}{r}$ Or $v \propto \frac{1}{\sqrt{r}}$	(1) (1) (1)	3
6(b)(ii)	State $T = \frac{2\pi}{\omega}$ and $\omega = \frac{v}{r}$ Or $T = \frac{s}{v}$ and $s = 2\pi r$ Hence $T = \frac{2\pi r}{v}$ (so smaller v leads to a larger value of T) [Accept $T = \frac{2\pi GM_E}{v^3}$ for final mark]	(1) (1)	2
6(c)	Use of $T = \sqrt{\frac{4\pi^2 r^3}{GM}}$ T = 5530 s [92 minutes] <u>Example of calculation</u> $T = \sqrt{\frac{4\pi^2 r^3}{GM}} = \sqrt{\frac{4\pi^2 (6360000 \text{ m} + 400000 \text{ m})^3}{6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2} \times 5.98 \times 10^{24} \text{ kg}}} = 5530 \text{ s}$	(1) (1)	2
6(d)	Max 2 As radius decreases: There is a transfer of gravitational potential energy to kinetic energy [Accept kinetic energy increases and gravitational potential energy decreases] Sum of kinetic and gravitational potential energy decreases Or satellite does work against frictional forces Or transfer of kinetic energy of satellite to thermal energy Or heating occurs	(1) (1)	2
Total for question			12